

REPETITION 22/09

$$A\vec{x} = \vec{b}$$

If A is invertible $\Rightarrow \vec{x} = A^{-1}\vec{b}$

The inverse A^{-1} :

$$\text{If } A = \begin{pmatrix} a & b \\ c & d \end{pmatrix} \Rightarrow A^{-1} = \frac{1}{\text{ad-bc}} \begin{pmatrix} d & -b \\ -c & a \end{pmatrix}$$

\swarrow
 $\det(A)$ determinant

Notice : A is invertible $\Leftrightarrow \det(A) \neq 0$

Theorem 3.8 The following is equivalent for an $n \times n$ matrix

- a/ A is invertible
- b/ A has n pivot positions
- c/ The equation $A\vec{x} = \vec{0}$ has only the trivial solution
- d/ The columns of A form a lin. independent set
- e/ The lin. transformation $T(\vec{x}) = A\vec{x}$ is one-to-one
- f/ The equation $A\vec{x} = \vec{b}$ has exactly one solution for each $\vec{b} \in \mathbb{R}^n$
- g/ The columns of A span \mathbb{R}^n
- h/ The lin. transformation $T(\vec{x}) = A\vec{x}$ is onto
- i/ A^T is invertible