



# My Research Interests

Hans Heum

**Two main interests:**

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1. Concrete security in systems with many users.

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1. Concrete security in systems with many users.
2. Concrete security of Post-Quantum Cryptography.

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Game  $\text{Guess}_{\mathcal{E}}$

procedure Initialize

$K \stackrel{\$}{\leftarrow} \mathcal{K}; b \stackrel{\$}{\leftarrow} \{0, 1\}$

procedure LR( $M_0, M_1$ )

return  $C \stackrel{\$}{\leftarrow} \mathcal{E}_K(M_b)$

procedure Finalize( $b'$ )

return  $(b == b')$

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- and its **advantage** is how much **better** it can do than just guessing randomly.

**Note: for all cryptosystems other than the One-Time Pad, there are adversaries with advantage larger than zero.**

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A system is said to be *secure* if, for any adversary  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}(\lambda) = \text{negl}(\lambda)$ .

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A system is said to be *secure* if, for any adversary  $\mathcal{A}$ ,  $\text{Adv}_{\mathcal{A}}(\lambda) = \text{negl}(\lambda)$ .

- Modern paradigm: **Concrete security**
  - We now care about the exact advantage, so that we can calculate exact security levels.



# Multi-User Security

(Research interest 1)

# Multi-Key Security Degradation



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- We now let the adversary attack any one of  $n$  systems.
- Question 1: What is the probability that **A** will crack **at least one** of the systems?
- Question 2: If she cracks one of them, how does that affect the security of the rest?



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**Proven fact:** Reductions of proofs of security from a system with  $n$  keys to a system with 1 key are lossy in general, losing a factor of  $n$ .

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$$\text{Adv}_{\mathcal{A}}^n(\lambda) \geq n \cdot \text{Adv}_{\mathcal{A}}^1(\lambda)$$

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$$\begin{aligned} \text{1 billion users: } n \approx 2^{30} & \Rightarrow \text{Adv}_{\mathcal{A}}^n(\lambda) = n \cdot \text{Adv}_{\mathcal{A}}^1(\lambda) \\ & = 2^{30} \cdot 2^{-64} \\ & = 2^{-34} \end{aligned}$$

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- Really only have 34 bits of security!

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- ... but what about their **composition**?



# What I'm currently looking at

- A **hybrid** system: KEM + DEM = PKE
- Each of these have a linear loss of security in the multi-user setting
- ... but what about their **composition**?

**Theorem 1.** *For every PKE adversary  $\mathcal{A}$ , there is a KEM adversary  $\mathcal{B}$  and a DEM adversary  $\mathcal{C}$ , such that*

$$\text{Adv}_{\text{PKE}}^{\text{LRIND-CCA},n}(\mathcal{A}) \leq 2 \cdot \text{Adv}_{\text{KEM}}^{\text{IND-CCA},n}(\mathcal{B}) + \text{Adv}_{\text{DEM}}^{\text{OT-LRIND-CCA},n}(\mathcal{C}). \quad (5)$$

# How (parts of) the proof looks

Game $G_0^n(\mathcal{A})$	Oracle $\text{Oenc}(i, j, m_0, m_1)$	Oracle $\text{Odec}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \text{s K.gen}$ $b_1, \dots, b_n \leftarrow \text{s } \{0, 1\}$ $\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \mathbf{cor} \leftarrow \emptyset$ $(j, b'_j) \leftarrow \text{s } \mathcal{A}(pk_1, \dots, pk_n)$ <b>return</b> $b_j = b'_j$	$(K, c_1) \leftarrow \text{s K.enc}(pk_i)$ $c_2 \leftarrow \text{D.enc}(K, m_{b_j})$ <b>append</b> $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$ <b>return</b> $\langle c_1, c_2 \rangle$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$ <b>return</b> $\perp$ $K \leftarrow \text{K.dec}(sk_i, c_1)$ <b>if</b> $K = \perp$ <b>return</b> $\perp$ $m \leftarrow \text{D.dec}(K, c_2)$ <b>return</b> $m$	<b>append</b> $i$ to <b>cor</b> <b>return</b> $sk_i$

# How (parts of) the proof looks

Game $G_0^n(\mathcal{A})$	Oracle $O_{\text{enc}}(i, j, m_0, m_1)$	Oracle $O_{\text{dec}}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$c_2 \leftarrow D.\text{enc}(K, m_{b_j})$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \mathbf{cor} \leftarrow \emptyset$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	$K \leftarrow K.\text{dec}(sk_i, c_1)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	<b>return</b> $\langle c_1, c_2 \rangle$	<b>if</b> $K = \perp$	
<b>return</b> $b_j = b'_j$		<b>return</b> $\perp$	
		$m \leftarrow D.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Game $G_1^n(\mathcal{A})$	Oracle $O_{\text{enc}}(i, j, m_0, m_1)$	Oracle $O_{\text{dec}}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$K' \leftarrow \mathcal{K}$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K'$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \mathbf{cor} \leftarrow \emptyset$	$c_2 \leftarrow D.\text{enc}(K', m_{b_j})$	$K \leftarrow \mathbf{K}_i[c_1]$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	<b>else</b>	
<b>return</b> $b_j = b'_j$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow K.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow D.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

# How (parts of) the proof looks

Game $G_0^n(\mathcal{A})$	Oracle $\text{Oenc}(i, j, m_0, m_1)$	Oracle $\text{Odec}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{b_j})$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \mathbf{cor} \leftarrow \emptyset$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	<b>return</b> $\langle c_1, c_2 \rangle$	<b>if</b> $K = \perp$	
<b>return</b> $b_j = b'_j$		<b>return</b> $\perp$	
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$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$K' \leftarrow \mathcal{K}$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K'$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \mathbf{cor} \leftarrow \emptyset$	$c_2 \leftarrow \text{D}.\text{enc}(K', m_{b_j})$	$K \leftarrow \mathbf{K}_i[c_1]$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	<b>else</b>	
<b>return</b> $b_j = b'_j$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Adversary $\mathcal{B}$	if $\mathcal{A}$ calls $\text{Oenc}(i, j, m_0, m_1)$	if $\mathcal{A}$ calls $\text{Odec}(i, \langle c_1, c_2 \rangle)$	if $\mathcal{A}$ calls $\text{Cor}(i)$
$d_1, \dots, d_n \leftarrow \mathcal{S}\{0, 1\}$	$(K, c_1) \leftarrow \text{Oenc}(i, j)$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	$sk_i \leftarrow \text{Cor}(i)$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K$	$K \leftarrow \mathbf{K}_i[c_1]$	<b>return</b> $sk_i$
$(j, d'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{d_j})$	<b>else</b>	
$b'_j \leftarrow \neg(d_j = d'_j)$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{Odec}(i, c_1)$	
<b>return</b> $(j, b'_j)$		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

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$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{b_j})$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \mathbf{cor} \leftarrow \emptyset$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	<b>return</b> $\langle c_1, c_2 \rangle$	<b>if</b> $K = \perp$	
<b>return</b> $b_j = b'_j$		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
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Game $G_1^n(\mathcal{A})$	Oracle $\text{Oenc}(i, j, m_0, m_1)$	Oracle $\text{Odec}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$K' \leftarrow \mathcal{K}$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K'$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \mathbf{cor} \leftarrow \emptyset$	$c_2 \leftarrow \text{D}.\text{enc}(K', m_{b_j})$	$K \leftarrow \mathbf{K}_i[c_1]$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	<b>else</b>	
<b>return</b> $b_j = b'_j$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
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Adversary $\mathcal{B}$	if $\mathcal{A}$ calls $\text{Oenc}(i, j, m_0, m_1)$	if $\mathcal{A}$ calls $\text{Odec}(i, \langle c_1, c_2 \rangle)$	if $\mathcal{A}$ calls $\text{Cor}(i)$
$d_1, \dots, d_n \leftarrow \mathcal{S}\{0, 1\}$	$(K, c_1) \leftarrow \text{Oenc}(i, j)$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	$sk_i \leftarrow \text{Cor}(i)$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K$	$K \leftarrow \mathbf{K}_i[c_1]$	<b>return</b> $sk_i$
$(j, d'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{d_j})$	<b>else</b>	
$b'_j \leftarrow \neg(d_j = d'_j)$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{Odec}(i, c_1)$	
<b>return</b> $(j, b'_j)$		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Adversary $\mathcal{C}$	if $\mathcal{A}$ calls $\text{Oenc}(i, j, m_0, m_1)$	if $\mathcal{A}$ calls $\text{Odec}(i, \langle c_1, c_2 \rangle)$	if $\mathcal{A}$ calls $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$c_2 \leftarrow \text{Oenc}(j, m_0, m_1)$	$i' \leftarrow \mathbf{K}_i[c_1]$	
$i' = 0$	$\mathbf{K}_i[c_1] \leftarrow i'$	$m \leftarrow \text{Odec}(i', c_2)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	$i' \leftarrow i' + 1$	<b>else</b>	
<b>return</b> $(j, b'_j)$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

# How (parts of) the proof looks

Game $G_0^n(\mathcal{A})$	Oracle $\text{Oenc}(i, j, m_0, m_1)$	Oracle $\text{Odec}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{b_j})$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \mathbf{cor} \leftarrow \emptyset$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	<b>return</b> $\langle c_1, c_2 \rangle$	<b>if</b> $K = \perp$	
<b>return</b> $b_j = b'_j$		<b>return</b> $\perp$	
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$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$K' \leftarrow \mathcal{K}$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K'$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \mathbf{cor} \leftarrow \emptyset$	$c_2 \leftarrow \text{D}.\text{enc}(K', m_{b_j})$	$K \leftarrow \mathbf{K}_i[c_1]$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	<b>else</b>	
<b>return</b> $b_j = b'_j$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Adversary $\mathcal{B}$	if $\mathcal{A}$ calls $\text{Oenc}(i, j, m_0, m_1)$	if $\mathcal{A}$ calls $\text{Odec}(i, \langle c_1, c_2 \rangle)$	if $\mathcal{A}$ calls $\text{Cor}(i)$
$d_1, \dots, d_n \leftarrow \mathcal{S}\{0, 1\}$	$(K, c_1) \leftarrow \text{Oenc}(i, j)$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	$sk_i \leftarrow \text{Cor}(i)$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K$	$K \leftarrow \mathbf{K}_i[c_1]$	<b>return</b> $sk_i$
$(j, d'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{d_j})$	<b>else</b>	
$b'_j \leftarrow \mathcal{A}(d_j = d'_j)$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{Odec}(i, c_1)$	
<b>return</b> $(j, b'_j)$		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Adversary $\mathcal{C}$	if $\mathcal{A}$ calls $\text{Oenc}(i, j, m_0, m_1)$	if $\mathcal{A}$ calls $\text{Odec}(i, \langle c_1, c_2 \rangle)$	if $\mathcal{A}$ calls $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$c_2 \leftarrow \text{Oenc}(j, m_0, m_1)$	$i' \leftarrow \mathbf{K}_i[c_1]$	
$i' = 0$	$\mathbf{K}_i[c_1] \leftarrow i'$	$m \leftarrow \text{Odec}(i', c_2)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	$i' \leftarrow i' + 1$	<b>else</b>	
<b>return</b> $(j, b'_j)$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

$$\begin{aligned}
 \text{Adv}_{\text{PKE}}^{\text{LRIND-CCA}, n}(\mathcal{A}) &:= 2 \cdot \Pr[\text{LRIND-CCA}_{\text{PKE}}^n(\mathcal{A}) = 1] - 1 \\
 &= 2 \cdot \Pr[G_0^n(\mathcal{A}) = 1] - 1 \\
 &= 2 (\Pr[G_0^n(\mathcal{A}) = 1] - \Pr[G_1^n(\mathcal{A}) = 1] + \Pr[G_1^n(\mathcal{A}) = 1]) - 1 \\
 &= 2 (\Pr[G_0^n(\mathcal{A}) = 1] - \Pr[G_1^n(\mathcal{A}) = 1]) + 2 \cdot \Pr[G_1^n(\mathcal{A}) = 1] - 1 \\
 &\leq 2 \cdot \text{Adv}_{\text{KEM}}^{\text{IND-CCA}, n}(\mathcal{B}) + \text{Adv}_{\text{DEM}}^{\text{OT-LRIND-CCA}, n}(\mathcal{C}).
 \end{aligned}$$

□

# How (parts of) the proof looks

Game $G_0^n(\mathcal{A})$	Oracle $\text{Oenc}(i, j, m_0, m_1)$	Oracle $\text{Odec}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{b_j})$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \text{cor} \leftarrow \emptyset$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	<b>return</b> $\langle c_1, c_2 \rangle$	<b>if</b> $K = \perp$	
<b>return</b> $b_j = b'_j$		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Game $G_1^n(\mathcal{A})$	Oracle $\text{Oenc}(i, j, m_0, m_1)$	Oracle $\text{Odec}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$K' \leftarrow \mathcal{K}$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K'$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \text{cor} \leftarrow \emptyset$	$c_2 \leftarrow \text{D}.\text{enc}(K', m_{b_j})$	$K \leftarrow \mathbf{K}_i[c_1]$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	<b>else</b>	
<b>return</b> $b_j = b'_j$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Adversary $\mathcal{C}$	if $\mathcal{A}$ calls $\text{Oenc}(i, j, m_0, m_1)$	if $\mathcal{A}$ calls $\text{Odec}(i, \langle c_1, c_2 \rangle)$	if $\mathcal{A}$ calls $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$c_2 \leftarrow \text{Oenc}(j, m_0, m_1)$	$i' \leftarrow \mathbf{K}_i[c_1]$	
$i' = 0$	$\mathbf{K}_i[c_1] \leftarrow i'$	$m \leftarrow \text{Odec}(i', c_2)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	$i' \leftarrow i' + 1$	<b>else</b>	
<b>return</b> $(j, b'_j)$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Adversary $\mathcal{B}$	if $\mathcal{A}$ calls $\text{Oenc}(i, j, m_0, m_1)$	if $\mathcal{A}$ calls $\text{Odec}(i, \langle c_1, c_2 \rangle)$	if $\mathcal{A}$ calls $\text{Cor}(i)$
$d_1, \dots, d_n \leftarrow \mathcal{S}\{0, 1\}$	$(K, c_1) \leftarrow \text{Oenc}(i, j)$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	$sk_i \leftarrow \text{Cor}(i)$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K$	$K \leftarrow \mathbf{K}_i[c_1]$	<b>return</b> $sk_i$
$(j, d'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{d_j})$	<b>else</b>	
$b'_j \leftarrow \mathbb{1}(d_j = d'_j)$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{Odec}(i, c_1)$	
<b>return</b> $(j, b'_j)$		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

$$\begin{aligned}
 \text{Adv}_{\text{PKE}}^{\text{LRIND-CCA}, n}(\mathcal{A}) &:= 2 \cdot \Pr[\text{LRIND-CCA}_{\text{PKE}}^n(\mathcal{A}) = 1] - 1 \\
 &= 2 \cdot \Pr[G_0^n(\mathcal{A}) = 1] - 1 \\
 &= 2 (\Pr[G_0^n(\mathcal{A}) = 1] - \Pr[G_1^n(\mathcal{A}) = 1] + \Pr[G_1^n(\mathcal{A}) = 1]) - 1 \\
 &= 2 (\Pr[G_0^n(\mathcal{A}) = 1] - \Pr[G_1^n(\mathcal{A}) = 1]) + 2 \cdot \Pr[G_1^n(\mathcal{A}) = 1] - 1 \\
 &\leq 2 \cdot \text{Adv}_{\text{KEM}}^{\text{IND-CCA}, n}(\mathcal{B}) + \text{Adv}_{\text{DEM}}^{\text{OT-LRIND-CCA}, n}(\mathcal{C}).
 \end{aligned}$$

□

... It gets complicated.

# How (parts of) the proof looks

Game $G_0^n(\mathcal{A})$	Oracle $\text{Oenc}(i, j, m_0, m_1)$	Oracle $\text{Odec}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{b_j})$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \text{cor} \leftarrow \emptyset$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	<b>return</b> $\langle c_1, c_2 \rangle$	<b>if</b> $K = \perp$	
<b>return</b> $b_j = b'_j$		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Game $G_1^n(\mathcal{A})$	Oracle $\text{Oenc}(i, j, m_0, m_1)$	Oracle $\text{Odec}(i, \langle c_1, c_2 \rangle)$	Oracle $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\langle c_1, c_2 \rangle \in \mathbf{C}_i$	append $i$ to <b>cor</b>
$b_1, \dots, b_n \leftarrow \mathcal{S}\{0, 1\}$	$K' \leftarrow \mathcal{K}$	<b>return</b> $\perp$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K'$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	
$\mathbf{C}_1, \dots, \mathbf{C}_n, \mathbf{J}_1, \dots, \mathbf{J}_n, \text{cor} \leftarrow \emptyset$	$c_2 \leftarrow \text{D}.\text{enc}(K', m_{b_j})$	$K \leftarrow \mathbf{K}_i[c_1]$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	append $\langle c_1, c_2 \rangle$ to $\mathbf{C}_i$ , $j$ to $\mathbf{J}_i$	<b>else</b>	
<b>return</b> $b_j = b'_j$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Adversary $\mathcal{B}$	if $\mathcal{A}$ calls $\text{Oenc}(i, j, m_0, m_1)$	if $\mathcal{A}$ calls $\text{Odec}(i, \langle c_1, c_2 \rangle)$	if $\mathcal{A}$ calls $\text{Cor}(i)$
$d_1, \dots, d_n \leftarrow \mathcal{S}\{0, 1\}$	$(K, c_1) \leftarrow \text{Oenc}(i, j)$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	$sk_i \leftarrow \text{Cor}(i)$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$\mathbf{K}_i[c_1] \leftarrow K$	$K \leftarrow \mathbf{K}_i[c_1]$	<b>return</b> $sk_i$
$(j, d'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	$c_2 \leftarrow \text{D}.\text{enc}(K, m_{d_j})$	<b>else</b>	
$b'_j \leftarrow \mathcal{A}(d_j = d'_j)$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{Odec}(i, c_1)$	
<b>return</b> $(j, b'_j)$		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

Adversary $\mathcal{C}$	if $\mathcal{A}$ calls $\text{Oenc}(i, j, m_0, m_1)$	if $\mathcal{A}$ calls $\text{Odec}(i, \langle c_1, c_2 \rangle)$	if $\mathcal{A}$ calls $\text{Cor}(i)$
$(pk_1, sk_1), \dots, (pk_n, sk_n) \leftarrow \mathcal{K}.\text{gen}$	$(K, c_1) \leftarrow \mathcal{K}.\text{enc}(pk_i)$	<b>if</b> $\mathbf{K}_i[c_1] \neq \emptyset$	<b>return</b> $sk_i$
$\mathbf{K}_1, \dots, \mathbf{K}_n \leftarrow \emptyset$	$c_2 \leftarrow \text{Oenc}(j, m_0, m_1)$	$i' \leftarrow \mathbf{K}_i[c_1]$	
$i' = 0$	$\mathbf{K}_i[c_1] \leftarrow i'$	$m \leftarrow \text{Odec}(i', c_2)$	
$(j, b'_j) \leftarrow \mathcal{A}(pk_1, \dots, pk_n)$	$i' \leftarrow i' + 1$	<b>else</b>	
<b>return</b> $(j, b'_j)$	<b>return</b> $\langle c_1, c_2 \rangle$	$K \leftarrow \text{K}.\text{dec}(sk_i, c_1)$	
		<b>if</b> $K = \perp$	
		<b>return</b> $\perp$	
		$m \leftarrow \text{D}.\text{dec}(K, c_2)$	
		<b>return</b> $m$	

$$\begin{aligned}
 \text{Adv}_{\text{PKE}}^{\text{LRIND-CCA}, n}(\mathcal{A}) &:= 2 \cdot \Pr[\text{LRIND-CCA}_{\text{PKE}}^n(\mathcal{A}) = 1] - 1 \\
 &= 2 \cdot \Pr[G_0^n(\mathcal{A}) = 1] - 1 \\
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 &= 2 (\Pr[G_0^n(\mathcal{A}) = 1] - \Pr[G_1^n(\mathcal{A}) = 1]) + 2 \cdot \Pr[G_1^n(\mathcal{A}) = 1] - 1 \\
 &\leq 2 \cdot \text{Adv}_{\text{KEM}}^{\text{IND-CCA}, n}(\mathcal{B}) + \text{Adv}_{\text{DEM}}^{\text{OT-LRIND-CCA}, n}(\mathcal{C}).
 \end{aligned}$$

□

... It gets complicated.  
(Also it's wrong.)



# Current status

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- It now looks like introducing key corruptions leads to an additional factor of  $n$  security loss...

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- It now looks like introducing key corruptions leads to an additional factor of  $n$  security loss...
- though we still hope to find a way to circumvent this.
- Provable security is important!
- and the devil's in the details.

# Quantum Cryptanalysis

(Research interest 2)

«In order to test the security of Post-Quantum Cryptography, you need people that continuously try to find quantum algorithms that break it. However, you would need someone with both a good grasp of Quantum Computing, ideally with a background in physics, as well as an intimate knowledge of what's happening in the field of cryptography, and right now these fields are mostly separate. [...] I really wish there were more people out there working on this.»

– Marco Tomamichel, Quantum information theorist,  
in conversation at QIP 2020.

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– Marco Tomamichel, Quantum information theorist,  
in conversation at QIP 2020.

**... that's me :)**



**Thank you.**

