## EXERCISES FOR MA8203 ALGEBRAIC GEOMETRY

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The numbered exercises come from Daniel Perrin's textbook.

Chapter I Exercises. Due 1 February

• 1

- 2
- 7, assume k is infinite
- 8

Chapter II Exercises. Due 1 March

- 1
- 5: you can use Macaulay2 to help find the resolution in part (c)

Chapter III Exercises. Due 15 March

- Exercises about sheaves from class.
  - (1) Let  $\mathcal{F}$  be a sheaf on a topological space X and let  $U \subseteq X$  be open. Show that  $\mathcal{F}|_U$  is a sheaf on U.
  - (2) Let  $\pi : X \to Y$  be a continuous map of topological spaces and let  $\mathcal{F}$  be a sheaf on X. Show that  $\pi_*\mathcal{F}$ , defined by  $\pi_*\mathcal{F}(V) = \mathcal{F}(\pi^{-1}(V))$ , is a sheaf on Y.
  - (3) Let  $\mathcal{F}$  be a sheaf of rings on a topological space X.
    - (a) If  $p \in X$ , show that  $\mathcal{F}_p$  is a ring.
    - (b) If  $(X, \mathcal{O}_X)$  is a ringed space, and  $\mathcal{F}$  is an  $\mathcal{O}_X$ -module, show that  $\mathcal{F}_p$  is an  $\mathcal{O}_{X,p}$ -module.
  - (4) Show that a sequence  $\mathcal{F}' \to \mathcal{F} \to \mathcal{F}''$  of sheaves of abelian groups on X is exact if and only if  $\mathcal{F}'(U) \to \mathcal{F}(U) \to \mathcal{F}''(U)$  is exact for every open set  $U \subseteq X$ .
- Exercises A, 1
- ...more to come