MA3408 Week 11 Drew Heard (drew.k.heard@ntnu.no) March 22, 2021

Question 1.

If $f: Y \to X$ is a continuous map and $\pi: E \to X$ is a U(n)-bundle, then $c_i(f^*\pi) = f^*c_i(\pi)$ for any i.

Remark: Note that f^* has two different meanings here, once as a vector bundle pullback, and once as the pullback of a cohomology class.

Question 2.

Show that $B(G \times H) \simeq BG \times BH$ (whenever this makes sense).

Question 3.

Compute the first Chern class of the Hopf bundle $S^1 \to S^2 \to S^3$.