

Formler og konvensjoner

$$\begin{aligned}
 x &= r \cos(\theta) &= \varrho \cos(\theta) \sin(\varphi), & 0 \leq r, \varrho \\
 y &= r \sin(\theta) &= \varrho \sin(\theta) \sin(\varphi), & 0 \leq \theta < 2\pi \\
 z &= z &= \varrho \cos(\varphi), & 0 \leq \varphi \leq \pi.
 \end{aligned}$$

$$ds = |\gamma'(t)| dt$$

$$dA = dx dy = r dr d\theta$$

$$d\sigma = |\mathbf{r}_s \times \mathbf{r}_t| ds dt$$

$$(d\sigma = |(z_x, z_y, -1)| dx dy \quad \text{for} \quad z = z(x, y))$$

$$dV = dx dy dz = r dr d\theta dz = \varrho^2 \sin(\varphi) d\varrho d\varphi d\theta$$

$$d\mathbf{r} = \gamma'(s) ds = \mathbf{T} ds = \frac{\gamma'(t)}{|\gamma'(t)|} |\gamma'(t)| dt$$

$$\text{curl}(\mathbf{F}) = \nabla \times \mathbf{F} = \left(\frac{\partial F_3}{\partial x_2} - \frac{\partial F_2}{\partial x_3}, \frac{\partial F_1}{\partial x_3} - \frac{\partial F_3}{\partial x_1}, \frac{\partial F_2}{\partial x_1} - \frac{\partial F_1}{\partial x_2} \right)$$

$$\iint_D \left(\frac{\partial Q}{\partial x} - \frac{\partial P}{\partial y} \right) dA = \int_{\partial A} P dx + Q dy$$

$$\iint_{\partial V} \mathbf{F} \cdot \mathbf{N} d\sigma = \iiint_V \text{div}(\mathbf{F}) dV$$

$$\int_{\partial S} \mathbf{F} \cdot \mathbf{T} ds = \iint_S \text{curl}(\mathbf{F}) \cdot \mathbf{N} d\sigma$$