## MA0301

## ELEMENTARY DISCRETE MATHEMATICS <br> NTNU, SPRING 2022

## Set 10

Deadline: Monday 28.03.2022, 23:59
Exercise 1. There are 18 mathematics majors and 325 computer science majors at a college.
a) In how many ways can two representatives be picked so that one is a mathematics major and the other is a computer science major?
b) In how many ways can one representative be picked that is either a mathematics major or a computer science major?

Exercise 2. How many bit strings are there of length 10 that both begin and end with a 1?
Exercise 3. Lewis, Zax: Exercise 22.1.
Exercise 4. Find the value of each of these quantities:
a) $P(6,3)$
b) $P(6,5)$
c) $P(8,1)$
d) $P(8,5)$
e) $P(8,8)$
f) $P(10,9)$

Exercise 5. Find the value of each of these quantities:
a) $C(5,1)$
b) $C(5,3)$
c) $C(8,4)$
d) $C(8,8)$
e) $C(8,0)$
f) $C(12,6)$

Exercise 6. In how many ways can a set of five letters be selected from the english alphabet?
Exercise 7. In how many ways can we select three students from a group of five students to stand in line for a picture? In how many ways can we arrange all five of these students for a picture?

Exercise 8. How many ways are there for four men and five women to stand in a line so that:
a) all men stand together?
b) all women stand together?

Exercise 9. Lewis, Zax: Exercise 23.1.
Exercise 10. A certain ice cream store has 31 flavors of ice cream available. In how many ways can we order a dozen ice cream cones if:
a) we do not want the same flavor more than once?
b) a flavor may be ordered as many as 12 times?

Exercise 11. Determine the number of integer solutions for $x_{1}+x_{2}+x_{3}+x_{4}+x_{5}<40$ where
a) $x_{i} \geq 0,1 \leq i \leq 5$.
b) $x_{i} \geq-3,1 \leq i \leq 5$.

