TMA4110
Calculus 3

Norwegian University of Science and Technology
Departement of Mathematical Sciences
Edwards \& Penney, section 1.2
$11,15,28$

## Edwards \& Penney, section 1.3

5,14

## Exam problems

A-4a Find all the complex third roots of $8 i$ (i.e. $\sqrt[3]{8 i}$ ), and write them in the form $a+i b$ for $a, b \in \mathbb{R}$. Graph the roots in the complex plane.

A-8 The motion of a mechanical system is given by the differential equation $m y^{\prime \prime}+k y=\cos \omega t$ where $m=2$ and $k=8$. For what values of $\omega$ will the solution $y(t)$ be unbounded as $t \rightarrow \infty$ ?

## Multiple-choice questions

1 Given

$$
y^{\prime \prime}+8 y^{\prime}+16 y=x^{2} e^{-4 x}
$$

Which of the following expressions for $y_{p}$ is the correct one to use in the method of undetermined coefficients?
A: $\quad y_{p}=e^{-4 x}\left(A x^{2}+B x+C\right)$
B: $\quad y_{p}=e^{-4 x}\left(A x^{3}+B x^{2}+C x\right)$
C: $\quad y_{p}=e^{-4 x} A x^{2}$
D: $y_{p}=e^{-4 x}\left(A x^{4}+B x^{3}+C x^{2}\right)$

2 Suppose that $z^{3}=2 e^{i \pi / 6}$. What is the smallest positive integer $n$, such that $z^{n}$ is a real number?
A: 6
B: 9
C: 18
D: 36

