

TMA4110 Calculus 3 Autumn 2010

Exercise set 5 – Week 39

Edwards & Penney, section 1.2

11,15,28

Edwards & Penney, section 1.3

 $5,\!14$

Exam problems

A-4a Find all the complex third roots of 8i (i.e. $\sqrt[3]{8i}$), and write them in the form a + ib for $\overline{a}, b \in \mathbb{R}$. Graph the roots in the complex plane.

A-8 The motion of a mechanical system is given by the differential equation $my'' + ky = \cos \omega t$ where m = 2 and k = 8. For what values of ω will the solution y(t) be unbounded as $t \to \infty$?

Multiple-choice questions

1 Given

$$y'' + 8y' + 16y = x^2 e^{-4x}$$

Which of the following expressions for y_p is the correct one to use in the method of undetermined coefficients?

$$\begin{array}{lll} \mathbf{A:} & y_p = e^{-4x}(Ax^2 + Bx + C) & & \\ \mathbf{B:} & y_p = e^{-4x}(Ax^3 + Bx^2 + Cx) \\ \mathbf{C:} & y_p = e^{-4x}Ax^2 & & \\ \mathbf{D:} & y_p = e^{-4x}(Ax^4 + Bx^3 + Cx^2) \\ \end{array}$$

2 Suppose that $z^3 = 2e^{i\pi/6}$. What is the smallest positive integer n, such that z^n is a real number? **A:** 6

C: 18 **B:** 9 **D:** 36